

The Plancherel theorem is valid for X being a Hilbert space (please read 'Hilbert' instead of Banach).